## Math 6140: Homework 9

- $1. \ 13.6: \ 6, \ 8, \ 11, \ 12$
- $2. \ 14.1: \ 5, \ 6, \ 8, \ 10$
- 3. Suppose  $\mathbb{K}/\mathbb{F}$  is Galois of degree p and suppose  $\mathbb{K} = \mathbb{F}(\alpha)$  with  $\alpha^p \in \mathbb{F}$ . Show that  $\mathbb{K}$  contains a primitive pth root of unity, and when p is prime  $\mathbb{K}$  has all of them.
- 4. Use  $e^{2\pi i/7} + e^{12\pi i/7}$  to find an explicit polynomial  $f(x) \in \mathbb{Q}[x]$  such that the Galois group of its splitting field over  $\mathbb{Q}$  has 3 elements.