## Math 3170: Homework 2

1. Let $T$ be a right triangle with side lengths $1 / \sqrt{2}$ and hypotenuse length 1 . Show that in any set of 17 points placed in $T$, there must be two that are at most $1 / 4$ apart.
Hint: This is similar to one of the exercises in Chapter 1.
2. Find a closed formula for

$$
\sum_{i=1}^{n} i(i+1)
$$

and prove the formula is correct.
3. Show that for each $n \in \mathbb{Z}_{\geq 1}$, one can partition a triangle into $3 n+1$ similar triangles.
4. How many 4-digit positive integers are there where all the integers are different?
5. There are $n$ couples invited to a banquet. Suppose there are some number of speeches given during the banquet, so that at most one member of each couple gives a talk. How many different sets of speakers could the evening have?
6. Andy and Brenda are playing dice. Andy throws 4 dice simultaneously. Andy wins if a 6 appears, and Brenda wins if no 6 appears. Who is more likely to win?
7. How many ways are there of placing pawns in an $n \times n$ chessboard such that every row and every column of the board has an even number of pawns?

