Math 1110: The Spirit and Uses of Mathematics

Review for Exam 1: ANSWERS IN RED

1. 19311

2. (a) 0,7 (b) 24,9 (c) 15,0 (d)15,7

3. (a) $3 \times 2 + 4 - 6 = 4$ (b) $4 \times 3 + 6 \div 2 = 15$ **3.** (2 + 4) - 6 = 12 $4 \times (3 + 6) \div 2 = 18$ **3.** (2 + 4 - 6) = 0 $4 \times (3 + 6) \div 2 = 18$ **3.** (2 + 4 - 6) = 0 **4. 4.**



- **5.** (a) 2,4,6,8,10 (b) The set is empty
- 6. (a) \emptyset , {Your 1110 instructor} (b) \emptyset , { α }, { β }, { γ }, { α , β }, { α , γ }, { β , γ }, { α , β , γ } (c) \emptyset

7. (a) (b) (c)

8. (a) arithmetic 12,14,16,18 100 2n (b) arithmetic 12,14,16,18 98 2(n-1) (c) arithmetic 26,31,36,41 246 1 + 5(n-1)

(d) geometric $3125,15625,78125,3906255^{49}5^{n-1}$ (e) geometric 1,1,1,111

(f) geometric 32,64,128,256 $2^{49} 2^{n-1}$ (g) neither 0,0,0,0 0 the *n*th term is 1 if *n* belongs to the sequence 2,5,9,14,20,27,... and 0 otherwise (h) geometric 5, -5, 5, -5, 5, $5(-1)^n$







(b) 2 (c) $T - (M \cup O)$

11. Dr. Slam bought 12 pair of cufflinks in bulk for \$20 total. Each additional pair cost him \$40. If he spent \$940 on his entire collection, how many pair of cufflinks does he have? He has 35 pair.

12. You can't divide a nonzero whole number by zero, because $a \div 0 = x$ would mean x0 = a, which is impossible if a is not zero. Also, you can't divide 0 by 0 because $0 \div 0 = x$ would mean x0 = 0, and since ANY x would make this work, you can't solve for x.

- **13.** \$1,045,000
- **14.** \$46,080,000
- 15. (a)



(b) Because of the symmetry in the Venn diagram.

(c)



(d)
$$A\Delta B = (A \cup B) \cap \overline{(A \cap B)}$$

- 16. (a) 6 (b) 7,8,9
- **17.** (a) 1, 2, 4, 8, 16 (b) 1, 2, 4, 7, 11 (c) 1, 2, 4, 5, 7, 8

18. Beware of inductive reasoning: things that look to be the same based on just checking a few cases may not always be the same.

19. (a) 36, 67, 98, 129

(b) 10, 20, 40, 80

- **20.** (a) $4 \cdot 3 \cdot 2 \cdot 1 = 24$ (b) $(2 \cdot 1) \cdot (4 \cdot 3 \cdot 2 \cdot 1) = 48$ (c) $4 \cdot (5 \cdot 4 \cdot 3 \cdot 2 \cdot 1) = 480$ (d) $4 \cdot 4 \cdot (4 \cdot 3 \cdot 2 \cdot 1) = 384$
- **21.** (a) $h = V \div (\ell \cdot d)$ (b) s = 3600h (c) $y = i \div 36$ (d) h = 168w