

Theorem 1. There exist non-isomorphic complete BA's  $A, B$  such that each can be completely embedded in the other. (This answers a question of T. Carlson.) Theorem 2. For each  $\kappa \geq \omega$  there is a BA  $A$  with no uncountable free subalgebra such that  ${}^{\omega}A$  has a free subalgebra of size  $\kappa$ . For the notion of tightness of a topological space, see Engelking's book; we apply it also to the dual BA. For any limit  $\kappa$  there is a BA of tightness  $\kappa$  not attained. But if  $\kappa$  is singular with  $\text{cf} \kappa = \omega$  then any BA of tightness  $\kappa$  has a free sequence of type  $\kappa$ , although when  $\text{cf} \kappa > \omega$  there are examples of non-attainment even in the free sequence sense. The algebra  $A$  of Theorem 2 has tightness  $\aleph_0$ ; since  $\text{independence}(A) \leq \text{tightness}(A)$ , this shows that  ${}^{\omega}A$  has tightness  $\geq \kappa$ . ( $\text{independence}(A) = \text{sup of cardinalities of free subalgebras of } A$ .) (Received September 22, 1980)

\*81T-A10 G.J. Rieger, Universität, D-3000 Hannover. On Farey-Ford triangles.

For every rational number in reduced form  $h/k$ , denote by  $C(h/k)$  the open circular disc (=Ford circle) in the cartesian plane with center  $(h/k, 1/(2k^2))$  and radius  $1/(2k^2)$  (see e.g. G.J. Rieger, Zahlen-theorie. Vandenhoeck und Ruprecht, Göttingen 1976; p. 140-142). Different Ford circles are disjoint and have a point of contact if and only if they belong to neighbors  $a/b < c/d$  in a suitable Farey sequence  $F_n$ ; the points  $(a/b, 0)$ ,  $(c/d, 0)$ , and the point  $((ab+cd)/(b^2+d^2), 1/(b^2+d^2))$  of contact form a right triangle  $T_n(a/b)$  (= Farey-Ford triangle). Denote by  $L_n$  the length of the polygon joining  $(0,0)$  with  $(1,0)$  along the legs of all  $T_n(a/b)$  with  $a/b \in F_n \cap [0,1[$ . Obviously,  $1 < L_n < \sqrt{2}$ . Theorem 1. There exists a real number  $\alpha (\approx 1,28)$  with  $L_n = \alpha + O(n^{-1}(\log n)^2)$  ( $n > 1$ ). We define the measure of a right triangle as height/hypotenuse. The measure  $M_n(a/b)$  of  $T_n(a/b)$  is  $bd/(b^2+d^2)$ . Theorem 2. The arithmetical mean of  $M_n(a/b)$  with  $a/b \in F_n \cap [0,1[$  is  $\beta + O(n^{-1} \log n)$  with  $\beta := 2 \int_0^1 \int_0^{1-x} xy(x^2+y^2)^{-1} dx dy$  ( $0 < x < 1, 0 < y < 1, x+y > 1$ ) =  $\log 2 + 1/2 - \pi/4$ . (Received September 22, 1980)

\*81T-A11 PRABIR DAS, Indian Statistical Institute, Calcutta 700 035, India. Characterization of unigraphic and unidigraphic degree sequences.

By degree of a vertex  $u$  of a digraph we mean the ordered pair ((outdegree of  $u$ ), (indegree of  $u$ )). Thus the degree sequence for both graphs and digraphs is the sequence of the degrees of the vertices. In this paper we characterize unigraphic degree sequences and, as a corollary, pairs of sequences with unique realization by bipartite graphs. These characterizations are alternate to those obtained by Koren in J. Combin. Theory 21B (1976), 224-234 and 235-244. Then we obtain characterizations for unidigraphic degree sequences and, as a corollary, for pairs of sequences with unique realization by bipartite digraphs. (Received September 24, 1980)

\*81T-A12 P. M. DEARING and NANCY V. PHILLIPS, Clemson University, Clemson, South Carolina 29631. Finding a minimum dominating set of a chordal graph.

We present three polynomial time algorithms to find a minimum dominating set [MDS] for a finite, simple undirected chordal graph. Two are applied to the graph and one to the node-node adjacency matrix representing the graph. Two are dual algorithms in that they construct a MDS by adding nodes until a feasible dominating set is obtained, while the third is a primal algorithm in that it starts with a feasible dominating set and deletes nodes until a MDS is obtained. (Received September 29, 1980) (Authors introduced by R. E. Jamison)

\*81T-A13 GLENN HOPKINS, The University of Mississippi, University, Mississippi 38677 and WILLIAM STATON, The University of Mississippi, University, Mississippi 38677. Extremal bipartite subgraphs of cubic triangle-free graphs.

Theorem: If  $G$  is a cubic graph with  $n$  vertices and if  $G$  contains no triangle, then there is a spanning bipartite subgraph  $H$  of  $G$  such that  $H$  has at least  $\frac{6n}{5}$  edges.

Examples are cited to show that this result is best possible. (Received September 29, 1980)