

**General Info**

*Instructor:* Professor David Grant, grant@colorado.edu

*Office Hours:* M 2-2:50, F 11-11:50 (or by appointment), in Math 303 (x2-7208).

*Class Meetings:* MWF 1–1:50 PM in ECCR 108.

*Text:* W. Trappe and L. Washington, *An Introduction to Cryptography with Coding Theory, Second Edition.* (Prentice-Hall)

**Prerequisites.** Linear Algebra.

**About the course.**

Two of the major problems in computer science or electrical engineering involve data transmission. They are: I) Making sure that someone can understand the message you send; and II) Making sure that they can not.

Problem (I) is the problem of coding. When transmitting a stream of zeros and ones, some errors may occur, reversing a zero to a one and visa versa. This can happen due to human error in transmission, or noise over a channel through which the message is sent. These errors occur with a certain probability, so our goal will be to build enough redundancy into our message that the receiver can detect or correct a certain percentage of errors. On the other hand, we do not want to build in too much redundancy, for then we would be wasting valuable bandwidth.

Problem (II) is the problem of cryptography. People can intercept messages, so the sender wants to make sure that only the intended receiver can understand the message. This could be done with both transmitter and receiver having a secret code book, but it's impractical for a bank to have a secret code set up with each of 20 million customers! So we will focus on so-called public key cryptography, whereby the method for encrypting a message is public knowledge, yet with high probability, it is only the receiver who knows how to decrypt the message.

Both the problems turn out to be very mathematical. Fortunately, the mathematics involved in elementary coding and cryptography — algebra and number theory — are old and well-developed branches of mathematics. Unfortunately, it is not easy for a student interested in coding and cryptography to learn this requisite mathematics!

So the goals of the course are to help computer science and electrical engineering students learn the necessary mathematics to study these fields in more depth (and continue on to courses like ECEN 5682 and CSCI 6268), while at the same time teaching math students some of the beautiful applications of algebra and number theory. Indeed, I believe that the theory not only helps people understand the applications, but the applications help people understand the theory.

**Course requirements and grading.**

This course will meet three days a week. Homework will be assigned weekly, and will be due the following Wednesday. (Graduate) Students enrolled in the 5440 version of the course will be given additional exercises, usually of a more abstract mathematical nature. All the assignments will appear on the website: euclid.colorado.edu/~grant/courses/5440/, as will the daily outline of the course.

There will be two hour exams during our regular class time and in our usual room. The first will be on September 29 and the second will be on Nov. 3. There will be a take-home final, due at the end of our regularly scheduled final exam time, 4 p.m. on Dec. 18. Your final grade in this course will be determined by your total score out of 600 possible points. These points are broken down as follows: Homeworks count for a total of 200 points, the two hour exams will each be worth 100 points, and the final exam will make up the remaining 200 points. The final will, unlike the hour exams, be cumulative, with an emphasis on the material covered after the second exam.

### **Topical outline of the course:**

We will cover the introductory Chapter 1, and spend some time on the Classical Cryptosystems of Chapter 2. We will cover Chapter 3, on number theory and finite fields in detail (this is the mathematics we need for the course). We will do all of Chapter 6 and 7 on the RSA and discrete log cryptosystems, and discuss part of Chapter 9 on digital signatures. We will then cover the long Chapter 18 on coding theory in detail.

### **Further reading and resources**

Cryptography (non-mathematical): The Code Book, S. Singh; The Codebreakers, D. Kahn.

Cryptography (mathematical): Cryptography, Theory and Practice, D. Stinson; Introduction to Cryptography, J. Buchmann; A Course in Number Theory and Cryptography, N. Koblitz; Algebraic Aspects of Cryptography, N. Koblitz.

Coding: A First Course in Coding Theory, R. Hill; Elements of Algebraic Coding Theory, L. Vermani; Introduction to Coding Theory, J. H. van Lint;

Number Theory: A Friendly Introduction to Number Theory, J. Silverman; The Theory of Numbers, G. H. Hardy and E. M. Wright; A Classical Introduction to Modern Number Theory, K. Ireland and M. Rosen.

Algebra: A First Course in Abstract Algebra, J. Fraleigh; Topics in Algebra, I. Herstein; Basic Algebra, I. II., N. Jacobson.

### **Et Cetera:**

The last day to drop a course without fee or a “W” on your transcript is Sept. 13. Also note that the last day to drop a class in MyCUInfo is Nov. 3.

Campus policy regarding religious observances requires that faculty make every effort to deal reasonably and fairly with all students who, because of religious obligations, have conflicts with scheduled exams, assignments or required attendance. Please inform me as soon as possible, and well in advance, should you need, due to religious obligations, to miss an exam, homework, or class.

Students and faculty each have responsibility for maintaining an appropriate learning environment. Those who fail to adhere to such behavioral standards may be subject to discipline. Professional courtesy and sensitivity are especially important with respect to individuals and topics dealing with race, color, national origin, sex,

pregnancy, age, disability, creed, religion, sexual orientation, gender identity, gender expression, veteran status, political affiliation or political philosophy. Class rosters are provided to the instructor with the student's legal name. I will gladly honor your request to address you by an alternate name or gender pronoun. Please advise me of this preference early in the semester so that I may make appropriate changes to my records. For more information, see the policies on classroom behavior ([www.colorado.edu/policies/student-classroom-and-course-related-behavior](http://www.colorado.edu/policies/student-classroom-and-course-related-behavior)) and the Student Code of Conduct ([www.colorado.edu/osccr/](http://www.colorado.edu/osccr/))

If you qualify for accommodations because of a disability, please submit your accommodation letter from Disability Services to me in a timely manner so that your needs can be addressed. Disability Services determines accommodations based on documented disabilities in the academic environment. Information on requesting accommodations is located on the Disability Services website

[www.colorado.edu/disabilityservices/students](http://www.colorado.edu/disabilityservices/students).

Contact Disability Services at 303-492-8671 or [dsinfo@colorado.edu](mailto:dsinfo@colorado.edu) for further assistance. If you have a temporary medical condition or injury, see Temporary Medical Conditions under the Students tab on the Disability Services website and discuss your needs with me.

All students enrolled in a University of Colorado Boulder course are responsible for knowing and adhering to the academic integrity policy

[www.colorado.edu/policies/academic-integrity-policy](http://www.colorado.edu/policies/academic-integrity-policy)

and a student Honor Code ([www.colorado.edu/honorcode/](http://www.colorado.edu/honorcode/)). Violations of the policy may include: plagiarism, cheating, fabrication, lying, bribery, threat, unauthorized access to academic materials, clicker fraud, resubmission, and aiding academic dishonesty. All incidents of academic misconduct will be reported to the Honor Code Council ([honor@colorado.edu](mailto:honor@colorado.edu); 303-735-2273). Students who are found responsible for violating the academic integrity policy will be subject to nonacademic sanctions from the Honor Code Council as well as academic sanctions from me. Additional information regarding the academic integrity policy can be found at the Honor Code Office website above. I will expect each student to sign the pledge of the honor code on each exam.

The University of Colorado Boulder (CU Boulder) is committed to maintaining a positive learning, working, and living environment. CU Boulder will not tolerate acts of sexual misconduct, discrimination, harassment or related retaliation against or by any employee or student. CU's Sexual Misconduct Policy prohibits sexual assault, sexual exploitation, sexual harassment, intimate partner abuse (dating or domestic violence), stalking or related retaliation. CU Boulder's Discrimination and Harassment Policy prohibits discrimination, harassment or related retaliation based on race, color, national origin, sex, pregnancy, age, disability, creed, religion, sexual orientation, gender identity, gender expression, veteran status, political affiliation or political philosophy. Individuals who believe they have been subject to misconduct under either policy should contact the Office of Institutional Equity and Compliance

(OIEC) at 303-492-2127. Information about the OIEC, the above referenced policies, and the campus resources available to assist individuals regarding sexual misconduct, discrimination, harassment or related retaliation can be found at the OIEC website ([www.colorado.edu/institutionalequity/](http://www.colorado.edu/institutionalequity/)).