Math 2001: PHW4

Due: February 10, 2016

- 1. From the book do:
 - 2.10: 2, 6, 10
 - 5: 4
 - 6: 4, 8, 14
- 2. Identify whether each of the following statements is true or false. If it is true, prove it. If it is false, then provide a counterexample.
 - (a) Let A, B, and C be sets. Then

$$(A \cap B) \cup C = A \cap (B \cup C).$$

- (b) If $a, b \in \mathbb{Z}_{\geq 1}$ and both \sqrt{a} and \sqrt{b} are irrational, then \sqrt{ab} is irrational.
- 3. A point (m, n) in \mathbb{R}^2 is a *lattice point* if both $m, n \in \mathbb{Z}$. Prove that the number of lattice points inside any circle centered at the origin is a number of the form 4k + 1 for some integer k (note that you don't have to say what k is).

Hint: For (a), split the set of lattice points into subsets, depending on the quadrants.