## Math 2001: PHW2

## Due: January 27, 2016

- 1. Consider the set of positive integers which give a remainder of 3 when divided by 4. Give two different descriptions of this set using set-builder notation.
- 2. From the book do problems:
  - (a) 1.1.A (numbers 4, 8, 12, 16)
  - (b) 1.5.3
- 3. Give examples of the following, or explain why they do not exist.
  - (a) An infinite set with a finite number of subsets,
  - (b) A finite set with an infinite number of subsets,
  - (c) A finite set with the same number of subsets and elements.
- 4. Let A be a set, and let B = P(A) be the power set of A. Is  $A \in B$  or  $A \subseteq B$ ? Justify your answer.
- 5. What is the number of subsets of the set  $\{\{1, 2, 3\}, \{1\}, \{1, 4\}, \{1, 4, 5, \{1, 2\}\}, \{1, 2, 3, 4\}\}$ ?
- 6. What is the number of subsets of  $\{a, b, c, d, e, f\}$  which all contain c? Generalize by determining how many subsets of  $\{1, 2, ..., n\}$  contain 1.