

# CALCULUS 3

September 15, 2010

## 1st TEST

**YOUR NAME:**

- |   |   |
|---|---|
| <input type="radio"/> <b>002</b> J. HARPER ..... (9AM)<br><input type="radio"/> <b>003</b> C. MESA ..... (10AM)<br><input type="radio"/> <b>004</b> A. SPINA ..... (11AM) | <input type="radio"/> <b>005</b> A. SPINA ..... (12PM)<br><input type="radio"/> <b>006</b> M. STACKPOLE ..... (1PM)<br><input type="radio"/> <b>007</b> P. NEWBERRY ..... (3PM) |
|---|---|

### SHOW ALL YOUR WORK

**final answers without any supporting work  
will receive no credit even if they are right!**

**No cheat-sheets allowed.**

**Partial credit** will be given for any **reasonable amount of work pointing in the right direction** towards the solution of your problem. You will not get any partial credit for memorizing formulas and not knowing how to use them, or for anything you write that is not directly related to the solution of your problem.

If your tests contains **more than one solution or answer** to a problem or part of a problem, and one of them is wrong, then it will be **the wrong one** the one that **counts** for your grading!

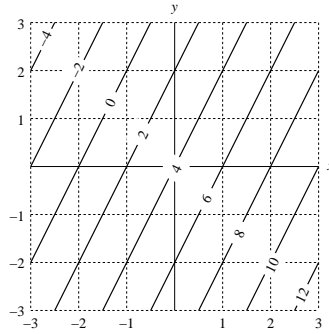
Make sure you write an arrow on top of vector quantities to differentiate them from scalar quantities (numbers). A word-processor and boldface fonts were used in writing test, but you are writing by hand! Remember that, within the same context,  $\vec{v}$  (with the arrow) is a *vector* ( $\vec{v} \equiv \mathbf{v}$ ) and  $v$  (without the arrow) is the *norm* of the previous vector ( $v \equiv \|\vec{v}\| \equiv \|\mathbf{v}\|$ ). If a vector is the null vector, write an arrow on top of the zero!

**DO NOT WRITE INSIDE THIS BOX!**

problem	points	score
1	15 pts	
2	15 pts	
3	15 pts	
4	15 pts	
5	15 pts	
6	10 pts	
7	15 pts	
8	15 pts	
9	15 pts	
<b>TOTAL</b>	100 pts	



3. [15 pts] Find the equation for the linear function with the contour diagram

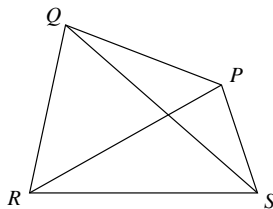


4. [15 pts] Describe the level curves of the function  $f(x, y) = |x| + |y|$ ,

5. [15 pts] Write each combination of vectors as a single vector, e.g.  $\vec{PQ}$ .

(a)  $\vec{PQ} + \vec{QR}$ ,      (b)  $\vec{RP} + \vec{PS}$ ,      (c)  $\vec{QS} - \vec{PS}$ ,      (d)  $\vec{RS} + \vec{SP} + \vec{PQ}$ .

You can use the figure below as a guide, if you need.



6. [10 pts] If  $\mathbf{v}$  lies in the first quadrant and makes an angle  $\pi/3$  with the positive  $y$ -axis and  $|\mathbf{v}| = 4$ , find  $\mathbf{v}$  in component form.

7. [15 pts] Show that

$$\frac{\mathbf{u}}{\|\mathbf{u}\|^2} - \frac{\mathbf{v}}{\|\mathbf{v}\|^2} \quad \text{and} \quad \frac{\mathbf{u}}{\|\mathbf{u}\| \|\mathbf{v}\|} - \frac{\mathbf{v}}{\|\mathbf{u}\| \|\mathbf{v}\|}$$

have the same magnitude, where  $\|\mathbf{u}\|$  and  $\|\mathbf{v}\|$  are nonzero vectors.

8. [15 pts] Use the vector product identity

$$\mathbf{a} \times (\mathbf{b} \times \mathbf{c}) = (\mathbf{a} \cdot \mathbf{c})\mathbf{b} - (\mathbf{a} \cdot \mathbf{b})\mathbf{c}$$

to evaluate

$$\mathbf{a} \times (\mathbf{b} \times \mathbf{c}) + \mathbf{b} \times (\mathbf{c} \times \mathbf{a}) + \mathbf{c} \times (\mathbf{a} \times \mathbf{b}).$$

9. [15 pts] Is the function

$$f(x, y) = \begin{cases} \frac{xy}{x^2 + xy + y^2} & \text{if } (x, y) \neq (0, 0) \\ 0 & \text{if } (x, y) = (0, 0) \end{cases}$$

continuous at  $(0, 0)$ ?